## Enthalpy and Internal Energy

- H or $\Delta H$ is used to symbolize enthalpy.
- The mathematical expression of the First Law of Thermodynamics is: $\Delta E=q+w$, where $\Delta E$ is the change in internal energy, $\boldsymbol{q}$ is heat and $\boldsymbol{w}$ is work.
- Work can be defined in terms of an expanding gas and has the formula: $w=-P \Delta V$, where $P$ is pressure in pascals $\left(\mathrm{N} / \mathrm{m}^{2}\right)$ and $\boldsymbol{V}$ is volume in $\mathrm{m}^{3}$.


## Enthalpy and Internal Energy

- Enthalpy (H) is related to energy.


$$
H=E+P V
$$

- However, absolute energies and enthalpies are rarely measured. Instead, we measure CHANGES in these quantities. Reconsider the above equations (at constant pressure):

$$
\begin{aligned}
& \Delta H=\Delta E+P \Delta V \\
& w=-P \Delta V \\
& \Delta H=\Delta E-w \\
& \Delta H=q+w-w \\
& \Delta H=q \quad \text { (at constant pressure) }
\end{aligned}
$$

recall:

$$
\text { therefore: } \quad \Delta H=\Delta E-w
$$

$$
\text { substituting: } \quad \Delta H=q+w-w
$$

- Therefore, at constant pressure, enthalpy is heat. We will use these words interchangeably.


## State Functions

- Enthalpy and internal energy are both STATE functions.
- A state function is path independent.
- Heat and work are both non-state functions.
- A non-state function is path dependant.


## Campsite B

$($ altitude $=4800 \mathrm{ft})$
$\triangle$
$\longrightarrow-$

Consider:
Location (position)

Distance traveled

Change in position

## Molar Enthalpy of Reactions $\left(\Delta \mathrm{H}_{\mathrm{rxn}}\right)$

- Heat $(\mathbf{q})$ is usually used to represent the heat produced $(-)$ or consumed (+) in the reaction of a specific quantity of a material.
- For example, q would represent the heat released when 5.95 g of propane is burned.
- The "enthalpy (or heat) of reaction" is represented by $\Delta H_{\text {reaction }}\left(\Delta H_{r x n}\right)$ and relates to the amount of heat evolved per one mole or a whole \# multiple - as in a balanced chemical equation.

$$
\text { molar } \Delta H_{\mathrm{rxn}}=\frac{\mathrm{q}_{\mathrm{rxn}}}{\text { moles reacting }} \quad \text { (in units of } \mathrm{kJ} / \mathrm{mol} \text { ) }
$$

## Enthalpy of Reaction

- Sometimes, however, knowing the heat evolved or consumed per gram is useful to know:
$\operatorname{gram} \Delta H_{r x n}=\frac{q_{r \times n}}{\text { grams reacting }}$
(in units of $\mathrm{J} / \mathrm{g}$ )


## Enthalpy of Reaction

7. Consider the combustion of hexene:

$$
\mathrm{C}_{6} \mathrm{H}_{12(\mathrm{I})}+9 \mathrm{O}_{2(\mathrm{~g})} \rightarrow 6 \mathrm{CO}_{2(\mathrm{~g})}+6 \mathrm{H}_{2} \mathrm{O}_{(\mathrm{g})}
$$

The combustion of 12.1 g of hexene in a calorimeter releases (exothermic, negative value) $44,700 \mathrm{~J}$ of heat.
A) What is the molar heat of combustion of hexene?
B) What is the gram heat of combustion of hexene?

## Enthalpy Change in Chemical Reactions: <br> Thermochemistry and Stoichiometry

- Heat may be considered as a reactant for endothermic reactions and as a product for exothermic reactions.
- In stoichiometry problems that involve heat, heat always keep the sign on $\Delta H$ to indicate whether heat is produced or consumed.

Example:
8. Consider the following endothermic reaction:
$4 \mathrm{NO}_{(\mathrm{g})}+6 \mathrm{H}_{2} \mathrm{O}_{(\mathrm{g})} \rightarrow 4 \mathrm{NH}_{3(\mathrm{~g})}+5 \mathrm{O}_{2(\mathrm{~g})} \quad \Delta \mathrm{H}^{\circ}=906.22 \mathrm{~kJ}$
What quantity of heat will be consumed when 58.0 g of $\mathrm{NH}_{3}$ is produced?

## Thermochemistry \& Limiting Reagents

- When carrying out stoichiometry problems that involve heat, all the same principles of stoichiometry apply, including Limiting Reagents.

Example:
9. How much heat is released when a mixture containing $10.0 \mathrm{~g} \mathrm{CS}_{2}$ and $10.0 \mathrm{~g} \mathrm{Cl}_{2}$ react by the equation:
$\mathrm{CS}_{2(\mathrm{~g})}+3 \mathrm{Cl}_{2(\mathrm{~g})} \rightarrow \mathrm{S}_{2} \mathrm{Cl}_{2(\mathrm{~g})}+\mathrm{CCl}_{4(\mathrm{~g})} \quad \Delta \mathrm{H}=-232 \mathrm{~kJ}$

## Enthalpy of Reactions - Summary

Heats of reaction $(\Delta H)$ can be calculated in one ōf three ways, all experimentally derived:

- Calorimetry (direct experiment)
- Hess's Law of Heat Summation
(using $\Delta H$ values of other reactions that were previously determined by experiment)
- Heats of Formation
(an application of Hess's Law)


## Determining the Enthalpy of Reactions

 by Calorimetry- All enthalpies of reaction must be determined experimentally, or calculated from the enthalpies of other reactions (which were experimentally determined and compiled in tables - see appendix L).
- We can use calorimetry to directly determine the enthalpy of a reaction, by measuring the heat transferred between a reaction (the system) to some defined surroundings (usually a calorimeter and water).


## Example: Determining the Enthalpy of

 Reactions by Calorimetry10. The $0.548-\mathrm{g}$ of arabinose, $\mathrm{C}_{5} \mathrm{H}_{10} \mathrm{O}_{5}$ is completely burned in oxygen in a calorimeter with a heat capacity of $825 \mathrm{~J} / \mathrm{C}^{\circ}$ and containing 3.58 kg of water. The temperature rises from $21.203^{\circ} \mathrm{C}$ to $21.743^{\circ} \mathrm{C}$.

What is the molar heat of combustion $(\Delta \mathrm{H})$ of arabinose?

## Example: Determining the Enthalpy of Reactions by Calorimetry

11) Consider the reaction of $10.08-\mathrm{g}$ of aluminum hydroxide with 200.0 mL of sulfuric acid solution with a concentration high enough to react all of the base.

If the reaction takes place in a coffee-cup calorimeter with a heat capacity of $63.5 \mathrm{~J} / \mathrm{C}^{\circ}$, and the temperature of all of the materials rise from $22.31^{\circ} \mathrm{C}$ to $28.52^{\circ} \mathrm{C}$, what is the heat of reaction $(\Delta \mathrm{H})$ for this neutralization reaction?
(Assume the density and the heat capacity of the solution are the same as water.)

## Hess's Law of Heat Summation

If a reaction is the sum of 2 or more reactions, then its overall $\Delta H$ is equal to the sum of the $\Delta H$ values of the other reactions.
12. Example: Consider the reaction for which $\Delta H$ is unknown:

$$
2 \mathrm{~S}_{(\mathrm{s})}+3 \mathrm{O}_{2(\mathrm{~g})} \rightarrow 2 \mathrm{SO}_{3(\mathrm{~g})}
$$

However, the heats of reaction of the following two reactions are known:

$$
\begin{array}{ll}
\mathrm{S}(\mathrm{~s})+\mathrm{O}_{2(\mathrm{~g})} \rightarrow \mathrm{SO}_{2(\mathrm{~g})} & \Delta \mathrm{H}=-297 \mathrm{~kJ} \\
2 \mathrm{SO}_{3(\mathrm{~g})} \rightarrow 2 \mathrm{SO}_{2(\mathrm{~g})}+\mathrm{O}_{2(\mathrm{~g})} & \Delta \mathrm{H}=198 \mathrm{~kJ}
\end{array}
$$

We can calculate the heat of reaction for the reaction for the unknown by combining these two reactions.

## Hess's Law Example

13. Consider the reaction:

$$
\mathrm{W}_{(\mathrm{s})}+\mathrm{C}_{(\mathrm{s}, \text { graphite })} \rightarrow \mathrm{WC}_{(\mathrm{s})}
$$

for which the heat of reaction is not known. Calculate $\Delta \mathrm{H}_{\text {rxn }}$ using the following information:
$2 \mathrm{~W}_{(\mathrm{s})}+3 \mathrm{O}_{2(\mathrm{~g})} \rightarrow 2 \mathrm{WO}_{3(\mathrm{~s})} \quad \Delta \mathrm{H}=-1680.6 \mathrm{~kJ}$
$\mathrm{C}_{\text {(graphite) }}+\mathrm{O}_{2(\mathrm{~g})} \rightarrow \mathrm{CO}_{2(\mathrm{~g})} \quad \Delta \mathrm{H}=-393.5 \mathrm{~kJ}$
$2 \mathrm{WC}_{(\mathrm{s})}+5 \mathrm{O}_{2(\mathrm{~g})} \rightarrow 2 \mathrm{WO}_{3(\mathrm{~s})}+2 \mathrm{CO}_{2(\mathrm{~g})} \quad \Delta \mathrm{H}=-2391.6 \mathrm{~kJ}$

## Enthalpy Diagram

(13 continued) Draw an energy diagram that illustrates the relationships of the $\Delta H$ values for each of above reaction. steps and the overall reaction.
$\Delta H$
(kJ)


## Hess's Law Example

Consider the gas-phase reaction:

$$
2 \mathrm{~N}_{2} \mathrm{O}_{5} \rightarrow 4 \mathrm{NO}_{2}+\mathrm{O}_{2}
$$

A) Based on the gas-phase reactions below with the enthalpies given, determine the $\Delta H$ value for the above reaction.

$$
\begin{array}{ll}
4 \mathrm{NO}+3 \mathrm{O}_{2} \rightarrow 2 \mathrm{~N}_{2} \mathrm{O}_{5} & \Delta \mathrm{H}=-445 \mathrm{~kJ} \\
2 \mathrm{NO}+\mathrm{O}_{2} \rightarrow 2 \mathrm{NO}_{2} & \Delta \mathrm{H}=-112 \mathrm{~kJ}
\end{array}
$$

## Enthalpy Diagram

B. (continued from previous slide) Draw an energy diagram that illustrates the relationships of the $\Delta \mathrm{H}$ values for each of above reaction steps and the overall reaction.


## Example continued

- What quantity of heat is produced or consumed by the decomposition of 25.0 g of dinitrogen pentoxide?


## Heats of Formation



- The standard molar enthalpy of formation for a compound is the amount of energy required to make one mole of a compound from its elements in their standard states.
- Thermodynamic standard conditions are defined:
- 1 atmosphere ( 760 mmHg ) pressure
- $25.00^{\circ} \mathrm{C}$ (298.15K)
- Solutions at 1.00 M


## Heats of Formation

- Consider HCl . The reaction that defines its standard enthalpy of formation is:
$1 / 2 \mathrm{H}_{2(\mathrm{~g})}+1 / 2 \mathrm{Cl}_{2(\mathrm{~g})} \rightarrow \mathrm{HCl}_{(\mathrm{g})} \quad \Delta \mathrm{H}_{\mathrm{rxn}}=-92.3 \mathrm{~kJ}$
- Therefore, $\Delta \mathrm{H}_{\mathrm{f}}^{\circ}=-92.3 \mathrm{~kJ} / \mathrm{mol}$. Note the units!
- The standard heat of formation of an element in its standard state is always defined as zero.


## STANDARD THERMODYNAMIC VALUES FOR SELECTED SUBSTANCES AT 298 K

| Substance or lon | $\Delta H_{f}^{0}$ <br> ( $\mathrm{kJ} / \mathrm{mol}$ ) | $\Delta G_{f}^{0}$ <br> (kJ/mol) | $\begin{aligned} & S^{0} \\ & (\mathrm{~J} / \mathrm{mol} \cdot \mathrm{~K}) \end{aligned}$ | Substance or Ion | $\Delta H_{f}^{0}$ <br> (kJ/mol) | $\Delta G_{f}^{0}$ <br> (kJ/mol) | $\begin{aligned} & S^{\circ} \\ & (\mathrm{J} / \mathrm{mol} \cdot \mathrm{~K}) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{e}^{-}(\mathrm{g})$ | 0 | 0 | 20.87 | $\mathrm{CaCO}_{3}(s)$ | - 1206.9 | - 1128.8 | 92.9 |
| Aluminum |  |  |  | $\mathrm{CaO}(\mathrm{s})$ | -635.1 | -603.5 | 38.2 |
| $\mathrm{Al}(\mathrm{s})$ | 0 | 0 | 28.3 | $\mathrm{Ca}(\mathrm{OH})_{2}(\mathrm{~s})$ | -986.09 | -898.56 | 83.39 |
| $\mathrm{Al}^{3+}(a q)$ | -524.7 | -481.2 | -313 | $\mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}(\mathrm{~s})$ | -4138 | -3899 | 263 |
| $\mathrm{AlCl}_{3}(s)$ | -704.2 | -628.9 | 110.7 | $\mathrm{CaSO}_{4}(s)$ | -1432.7 | -1320.3 | 107 |
| $\mathrm{Al}_{2} \mathrm{O}_{3}(\mathrm{~s})$ | -1676 | -1582 | 50.94 | Carbon |  |  |  |
| Barium |  |  |  | C(graphite) | 0 | 0 | 5.686 |
| $\mathrm{Ba}(\mathrm{s})$ | 0 | 0 | 62.5 | C(diamond) | 1.896 | 2.866 | 2.439 |
| $\mathrm{Ba}(\mathrm{g})$ | 175.6 | 144.8 | 170.28 | $\mathrm{C}(\mathrm{g})$ | 715.0 | 669.6 | 158.0 |
| $\mathrm{Ba}^{2+}(\mathrm{g})$ | 1649.9 | - | - | $\mathrm{CO}(\mathrm{g})$ | -110.5 | -137.2 | 197.5 |
| $\mathrm{Ba}^{2+}(a q)$ | -538.36 | -560.7 | 13 | $\mathrm{CO}_{2}(\mathrm{~g})$ | -393.5 | -394.4 | 213.7 |
| $\mathrm{BaCl}_{2}(\mathrm{~s})$ | -806.06 | -810.9 | 126 | $\mathrm{CO}_{2}(\mathrm{aq})$ | -412.9 | -386.2 | 121 |
| $\mathrm{BaCO}_{3}(s)$ | -1219 | -1139 | 112 | $\mathrm{CO}_{3}{ }^{2-}(\mathrm{aq})$ | -676.26 | -528.10 | -53.1 |
| $\mathrm{BaO}(s)$ | -548.1 | -520.4 | 72.07 | $\mathrm{HCO}_{3}{ }^{-}(\mathrm{aq})$ | -691.11 | 587.06 | 95.0 |
| $\mathrm{BaSO}_{4}(s)$ | -1465 | -1353 | 132 | $\mathrm{H}_{2} \mathrm{CO}_{3}(a q)$ | -698.7 | -623.42 | 191 |
| Boron |  |  |  | $\mathrm{CH}_{4}(\mathrm{~g})$ | -74.87 | -50.81 | 186.1 |
| B ( $\beta$-rhombo- | 0 | 0 | 5.87 | $\mathrm{C}_{2} \mathrm{H}_{2}(\mathrm{~g})$ | 227 | 209 | 200.85 |
| hedral) |  |  |  | $\mathrm{C}_{2} \mathrm{H}_{4}(\mathrm{~g})$ | 52.47 | 68.36 | 219.22 |
| $\mathrm{BF}_{3}(\mathrm{~g})$ | -1137.0 | $-1120.3$ | 254.0 | $\mathrm{C}_{2} \mathrm{H}_{6}(\mathrm{~g})$ | -84.667 | -32.89 | 229.5 |
| $\mathrm{BCl}_{3}(\mathrm{~g})$ | -403.8 | -388.7 | 290.0 | $\mathrm{C}_{3} \mathrm{H}_{8}(\mathrm{~g})$ | -105 | -24.5 | 269.9 |
| $\mathrm{B}_{2} \mathrm{H}_{6}(\mathrm{~g})$ | 35 | 86.6 | 232.0 | $\mathrm{C}_{4} \mathrm{H}_{10}(\mathrm{~g})$ | -126 | -16.7 | 310 |
| $\mathrm{B}_{2} \mathrm{O}_{3}(\mathrm{~s})$ | -1272 | -1193 | 53.8 | $\mathrm{C}_{6} \mathrm{H}_{6}$ (I) | 49.0 | 124.5 | 172.8 |
| $\mathrm{H}_{3} \mathrm{BO}_{3}(s)$ | -1094.3 | -969.01 | 88.83 | $\mathrm{CH}_{3} \mathrm{OH}(\mathrm{g})$ | -201.2 | -161.9 | 238 |

## Calculating Heats of Reaction from $\Delta H$

- The heat of a reaction can be calculated by the following formula:
$\Delta \mathrm{H}_{\mathrm{rxn}}^{\circ}=\Sigma \mathrm{n}_{\mathrm{p}} \Delta \mathrm{H}_{\mathrm{f}, \text { products }}^{\circ}-\Sigma \mathrm{n}_{\mathrm{r}} \Delta \mathrm{H}_{\mathrm{f}, \text { reactants }}^{\circ}$ where $n_{x}$ is the stoichiometric coefficient.

14. Calculate the heat of reaction for the following reactions. (A chart of standard heats of formation can be found in appendix L.)

$$
\begin{aligned}
& 2 \mathrm{HNO}_{3(\mathrm{aq})}+\mathrm{NO}_{(\mathrm{g})} \rightarrow 3 \mathrm{NO}_{2(\mathrm{~g})}+\mathrm{H}_{2} \mathrm{O}_{(\mathrm{l})} \\
& 4 \mathrm{NH}_{3(\mathrm{~g})}+5 \mathrm{O}_{2(\mathrm{~g})} \rightarrow 4 \mathrm{NO}_{(\mathrm{g})}+6 \mathrm{H}_{2} \mathrm{O}_{(\mathrm{g})}
\end{aligned}
$$

## Heats of Formation - Applied

Calculate what quantity of heat that will be absorbed or released when 15.0 g of silver chloride $(\mathrm{AgCl})$ is converted to silver oxide $\left(\mathrm{Ag}_{2} \mathrm{O}\right)$ in the following reaction:
$4 \mathrm{AgCl}_{(\mathrm{s})}+\mathrm{O}_{2(\mathrm{~g})} \rightarrow 2 \mathrm{Ag}_{2} \mathrm{O}_{(\mathrm{s})}+2 \mathrm{Cl}_{2(\mathrm{~g})}$

Thermochemistry - Applied Example

A 2.21-g sample of $\mathrm{C}_{2} \mathrm{H}_{2}$ is burned in excess oxygen in a bomb calorimeter with a heat capacity of $453 \mathrm{~J} / \mathrm{C}^{\circ}$ that contains 250.0 g of water. What increase in temperature should be observed?
(Assume that ALL reactants and products are in the gaseous state.)

## Thermochemistry - Applied Example

Consider the reaction of:

- 100.0 mL of $0.500 \mathrm{MBa}\left(\mathrm{NO}_{3}\right)_{2}$ with 100.0 mL of $1.00 \mathrm{M} \mathrm{Na}_{2} \mathrm{SO}_{4}$ solution to form solid $\mathrm{BaSO}_{4}$.

Both solutions start at $25.05^{\circ} \mathrm{C}$ and are mixed in a calorimeter that absorbs a negligible quantity of heat. The final temperature of the mixture is $28.15^{\circ} \mathrm{C}$.

- What is the enthalpy $(\Delta \mathrm{H})$ of the reaction?
(Assume the density and specific heat of the solution are the same as water.)

