Math 222
Functions and Rate of Change

| Show all relevant work! |
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1. (a) Sketch pictures of (1) an increasing function and (2) a decreasing function.
(b) Write definitions for increasing and decreasing functions in terms of the independent variable $(x)$ and the dependent variable ( $y$ ).
2. Use the table below to answer the following questions:

| $x$ | 0 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 9 | 8 | 5 | 0 | -7 |

(a) find $f(4)$
(b) Solve $f(x)=0$
(c) Find the average rate of change from $x=0$ to $x=2$ and then from $x=2$ to $x=4$. What do you observe from your results?
3. The population of Half Moon Bay since 1995 can be modeled by the function $P(t)=10000(1.012)^{t}$ where $t$ is in years. Find the average rate of growth in population from 1995 to 1997 and from 1999 to 2001. What do you observe from your results?
4. Use the exponential function, $g(x)$, graphed below to answer the given questions.
(a) Estimate the average rate of change between $x=-2$ and $x=0$.
(b) Estimate the average rate of change between $x=0$ and $x=2$.
(c) Estimate $g(1)$.
(d) Estimate the solution to $g(x)=7$.


5 . Write formulas for the average rate of change from $x_{1}$ to $x_{2}$ and from $x_{2}$ to $x_{3}$ in each function. Discuss the qualitative changes in rates of change (positive to negative, relative size).
(a)

(b)


